Observation of an anomalous line shape of the $\eta' \pi^+ \pi^-$ mass spectrum near the $p\bar{p}$ mass threshold in $J/\psi \to \gamma \eta' \pi^+ \pi^-$

U. Zhang, C. C. Zhang, D. H. Zhang, H. H. Zhang, H. H. Zhang, J. L. Zhang, J. S. Zhang, J. D. Zhang, J. E. Zhang, J. Z. Zhang, J. Y. Zhang, J. Z. Zhang, J. Zhang, J. Z. Zhang, J. Zhang, J. Z. Zhang, J. Z. Zhang, J. Z. Zhang, J. J. W. Zhao¹, J. F. Zhao¹, J. Z. Zhao⁴, Lei Zhao⁴, Lei Zhao⁴, M. G. Zhao⁴, Q. Zhao⁴, Q. W. Zhao⁵, S. J. Zhao⁴,
 T. C. Zhao¹, Y. B. Zhao^{1,a}, Z. G. Zhao^{46,a}, A. Zhemchugov^{23,c}, B. Zheng⁴⁷, J. P. Zheng^{1,a}, W. J. Zheng³³, Y. H. Zheng⁴¹,
 B. Zhong²⁸, L. Zhou^{1,a}, X. Zhou⁵¹, X. K. Zhou^{46,a}, X. R. Zhou^{46,a}, X. Y. Zhou¹, K. Zhu¹, K. J. Zhu^{1,a}, S. Zhu¹,
 S. H. Zhu⁴⁵, X. L. Zhu³⁹, Y. C. Zhu^{46,a}, Y. S. Zhu¹, Z. A. Zhu¹, J. Zhuang^{1,a}, L. Zotti^{49A,49C}, B. S. Zou¹, J. H. Zou¹

(BESIII Collaboration)

¹ Institute of High Energy Physics, Beijing 100049, People's Republic of China

² Beihang University, Beijing 100191, People's Republic of China

³ Beijing Institute of Petrochemical Technology, Beijing 102617, People's Republic of China

⁴ Bochum Ruhr-University, D-44780 Bochum, Germany

⁵ Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA

⁶ Central China Normal University, Wuhan 430079, People's Republic of China

⁷ China Center of Advanced Science and Technology, Beijing 100190, People's Republic of China

⁸ COMSATS Institute of Information Technology, Lahore, Defence Road, Off Raiwind Road, 54000 Lahore, Pakistan

⁹ G.I. Budker Institute of Nuclear Physics SB RAS (BINP), Novosibirsk 630090, Russia

¹⁰ GSI Helmholtzcentre for Heavy Ion Research GmbH, D-64291 Darmstadt, Germany

Guangxi Normal University, Guilin 541004, People's Republic of China

¹² GuangXi University, Nanning 530004, People's Republic of China

¹³ Hangzhou Normal University, Hangzhou 310036, People's Republic of China

¹⁴ Helmholtz Institute Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany

¹⁵ Henan Normal University, Xinxiang 453007, People's Republic of China

¹⁶ Henan University of Science and Technology, Luoyang 471003, People's Republic of China

¹⁷ Huangshan College, Huangshan 245000, People's Republic of China

¹⁸ Hunan University, Changsha 410082, People's Republic of China

¹⁹ Indiana University, Bloomington, Indiana 47405, USA

²⁰ (A)INFN Laboratori Nazionali di Frascati, I-00044, Frascati, Italy;

(B)INFN and University of Perugia, I-06100, Perugia, Italy

²¹ (A)INFN Sezione di Ferrara, I-44122, Ferrara, Italy; (B)University of Ferrara, I-44122, Ferrara, Italy

Johannes Gutenberg University of Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany

²³ Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia

²⁴ Justus-Liebig-Universitaet Giessen, II. Physikalisches Institut, Heinrich-Buff-Ring 16, D-35392 Giessen, Germany

²⁵ KVI-CART, University of Groningen, NL-9747 AA Groningen, The Netherlands

²⁶ Lanzhou University, Lanzhou 730000, People's Republic of China

²⁷ Liaoning University, Shenyang 110036, People's Republic of China

²⁸ Nanjing Normal University, Nanjing 210023, People's Republic of China

²⁹ Nanjing University, Nanjing 210093, People's Republic of China

³⁰ Nankai University, Tianjin 300071, People's Republic of China

³¹ Peking University, Beijing 100871, People's Republic of China

³² Seoul National University, Seoul, 151-747 Korea

³³ Shandong University, Jinan 250100, People's Republic of China

³⁴ Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China

³⁵ Shanxi University, Taiyuan 030006, People's Republic of China

³⁶ Sichuan University, Chengdu 610064, People's Republic of China

³⁷ Soochow University, Suzhou 215006, People's Republic of China

³⁸ Sun Yat-Sen University, Guangzhou 510275, People's Republic of China

³⁹ Tsinghua University, Beijing 100084, People's Republic of China

⁴⁰ (A)Ankara University, 06100 Tandogan, Ankara, Turkey; (B)Istanbul Bilgi University, 34060 Eyup, Istanbul, Turkey;

(C)Uludag University, 16059 Bursa, Turkey; (D)Near East University, Nicosia, North Cyprus, Mersin 10, Turkey

⁴¹ University of Chinese Academy of Sciences, Beijing 100049, People's Republic of China

⁴³ University of Minnesota, Minneapolis, Minnesota 55455, USA

⁴⁴ University of Rochester, Rochester, New York 14627, USA

⁴⁵ University of Science and Technology Liaoning, Anshan 114051, People's Republic of China

⁴⁶ University of Science and Technology of China, Hefei 230026, People's Republic of China

⁴⁷ University of South China, Hengyang 421001, People's Republic of China

⁸ University of the Punjab, Lahore-54590, Pakistan

⁴⁹ (A)University of Turin, I-10125, Turin, Italy; (B)University of Eastern

Piedmont, I-15121, Alessandria, Italy; (C)INFN, I-10125, Turin, Italy

⁵⁰ Uppsala University, Box 516, SE-75120 Uppsala, Sweden

⁵¹ Wuhan University, Wuhan 430072, People's Republic of China

⁵³ Zhengzhou University, Zhengzhou 450001, People's Republic of China

^a Also at State Key Laboratory of Particle Detection and Electronics, Beijing 100049, Hefei 230026, People's Republic of China ^b Also at Bogazici University, 34342 Istanbul, Turkey

^c Also at the Moscow Institute of Physics and Technology, Moscow 141700, Russia

^d Also at the Functional Electronics Laboratory, Tomsk State University, Tomsk, 634050, Russia

^e Also at the Novosibirsk State University, Novosibirsk, 630090, Russia

^f Also at the NRC "Kurchatov Institute", PNPI, 188300, Gatchina, Russia ^g Also at University of Texas at Dallas, Richardson, Texas 75083, USA

^h Also at Istanbul Arel University, 34295 Istanbul, Turkey

ⁱ Currently at DESY, 22607 Hamburg, Germany

Using $1.09 \times 10^9 J/\psi$ events collected by the BESIII experiment in 2012, we study the $J/\psi \rightarrow$ $\gamma \eta' \pi^+ \pi^-$ process and observe a significant abrupt change in the slope of the $\eta' \pi^+ \pi^-$ invariant mass distribution at the proton-antiproton $(p\bar{p})$ mass threshold. We use two models to characterize the $\eta' \pi^+ \pi^-$ line shape around 1.85 GeV/ c^2 : one which explicitly incorporates the opening of a decay threshold in the mass spectrum (Flatté formula), and another which is the coherent sum of two resonant amplitudes. Both fits show almost equally good agreement with data, and suggest the

⁵² Zhejiang University, Hangzhou 310027, People's Republic of China

42 University of Hawaii, Honolulu, Hawaii 96822, USA

existence of either a broad state around 1.85 GeV/c^2 with strong couplings to $p\bar{p}$ final states or a narrow state just below the $p\bar{p}$ mass threshold. Although we cannot distinguish between the fits, either one supports the existence of a $p\bar{p}$ molecule-like state or bound state with greater than 7σ significance.

PACS numbers: 12.39.Mk, 12.40.Yx, 13.20.Gd, 13.75.Cs

The state X(1835) was first observed by the BESII experiment as a peak in the $\eta' \pi^+ \pi^-$ invariant mass distribution in $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$ decays [1]. This observation was later confirmed by BESIII studies of the same process [2] with mass and width measured to be $M = 1836.5 \pm 3^{+5.6}_{-2.1} \text{ MeV}/c^2$ and $\Gamma = 190 \pm 9^{+38}_{-36} \text{ MeV}/c^2$; the X(1835) was also observed in the $\eta K^0_S K^0_S$ channel in $J/\psi \to \gamma \eta K_S^0 K_S^0$ decays, where its spin-parity was determined to be $J^P = 0^-$ by a partial wave analysis (PWA) [3]. An anomalously strong enhancement at the proton-antiproton $(p\bar{p})$ mass threshold, dubbed $X(p\bar{p})$, was first observed by BESII in $J/\psi \to \gamma p\bar{p}$ decays [4]; this observation was confirmed by BESIII [5] and CLEO [6]. This enhancement structure was subsequently determined to have spin-parity $J^P = 0^-$ by BESIII [7]. Among the various theoretical interpretations on the nature of the X(1835) and $X(p\bar{p})$ [8–12], a particularly intriguing one suggests that the two structures originate from a $p\bar{p}$ bound state [13–17]. If the X(1835) is really a $p\bar{p}$ bound state, it should have a strong coupling to $0^- p\bar{p}$ systems, in which case the line shape of X(1835) at the $p\bar{p}$ mass threshold would be affected by the opening of the $X(1835) \rightarrow p\bar{p}$ decay mode. A study of the $\eta' \pi^+ \pi^$ line shape of X(1835) with high statistical precision therefore provides valuable information that helps clarify the nature of the X(1835) and $X(p\bar{p})$.

In this Letter, we report the observation of a significant abrupt change in slope of the $X(1835) \rightarrow \eta' \pi^+ \pi^-$ line shape at the $p\bar{p}$ mass threshold in a sample of $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$ events collected in the BESIII detector at the BEPCII e^+e^- storage ring. The η' is reconstructed in its two major decay modes: $\eta' \rightarrow \gamma \pi^+ \pi^-$ and $\eta' \rightarrow \eta \pi^+ \pi^-$, $\eta \rightarrow \gamma \gamma$. The data sample used in this analysis contains a total of $1.09 \times 10^9 J/\psi$ decay events [18] accumulated by the BESIII experiment in 2012.

The BESIII detector [19] is a magnetic spectrometer operating at BEPCII [20], a double-ring e^+e^- collider with center of mass energies between 2.0 and 4.6 GeV. The cylindrical core of the BESIII detector consists of a helium-based main drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC) that are all enclosed in a superconducting solenoidal magnet providing a 0.9 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identifier modules interleaved with steel. The acceptance of charged particles and photons is 93% of the 4π solid angle. The charged-particle momentum resolution at 1 GeV/c is 0.5%; the EMC measures 1 GeV photons with an energy resolution of 2.5% (5%) in the barrel (end cap) regions. A GEANT4-based [21] Monte Carlo (MC) simulation software package is used to optimize the event selection criteria, estimate backgrounds, and determine the detection efficiency. The KKMC [22] generator is used to simulate J/ψ production.

Charged tracks are reconstructed using hits in the MDC. The point of closest approach of each charged track to the e^+e^- interaction point is required to be within 20 cm in the beam direction and 2 cm in the plane perpendicular to the beam direction. The reconstructed polar angle between the charged-track and beam direction is restricted to $|\cos \theta| < 0.93$. The TOF and energy loss (dE/dx) information are combined to form particle identification confidence levels for the π , K, and p hypotheses; each track is assigned to the particle type that corresponds to the hypothesis with the highest confidence level. Photon candidates are selected from showers in the EMC with energy deposited in the EMC barrel ($|\cos \theta| < 0.8$) or end-cap regions ($0.86 < |\cos \theta| <$ 0.92) to be greater than 100 MeV. EMC cluster timing requirements are used to suppress electronic noise and energy deposits that are unrelated to the event.

To select events from $J/\psi \to \gamma \eta' \pi^+ \pi^-$, four charged tracks with zero net charge are required. Among the four tracks, at least three of them should be positively identified as pions. At least two photon candidates are required for the $\eta' \to \gamma \pi^+ \pi^-$ mode; three photon candidates are required for the $\eta' \to \eta \pi^+ \pi^-$, $\eta \to \gamma \gamma$ mode.

For the $J/\psi \rightarrow \gamma \eta' (\rightarrow \gamma \pi^+ \pi^-) \pi^+ \pi^-$ channel, a four-constraint (4C) kinematic fit which imposes energy and momentum conservation is performed to the $\gamma \gamma \pi^+ \pi^- \pi^+ \pi^-$ hypothesis; the χ^2_{4C} of the kinematic fit is required to be smaller than 40. If there are more than two photon candidates, the two-photon combination with the smallest χ^2_{4C} value is retained. Events with: $|M_{\gamma\gamma} - m_{\pi^0}| < 40 \text{ MeV}/c^2$; $|M_{\gamma\gamma} - m_{\eta}| < 30 \text{ MeV}/c^2$; 720 MeV/ $c^2 < M_{\gamma\gamma} < 820 \text{ MeV}/c^2$; or 400 MeV/ $c^2 < M_{\gamma \pi^+ \pi^-} < 563$ MeV/ c^2 are rejected to suppress background events from: $J/\psi \to \pi^0 \pi^+ \pi^- \pi^+ \pi^-$; $J/\psi \rightarrow \eta \pi^+ \pi^- \pi^+ \pi^-; J/\psi \rightarrow \omega (\rightarrow \gamma \pi^0) \pi^+ \pi^- \pi^+ \pi^-;$ and $J/\psi \to \gamma \eta (\to \gamma \pi^+ \pi^-, \pi^0 \pi^+ \pi^-) \pi^+ \pi^-$, respectively. Finally, the η' is reconstructed by a $\gamma \pi^+ \pi^-$ combination that satisfies both $|M_{\pi^+\pi^-} - m_{\rho^0}| < 200 \text{ MeV}/c^2$ and $|M_{\gamma\pi^+\pi^-} - m_{\eta'}| < 15 \text{ MeV}/c^2$. If two or more combinations pass these two criteria, the one with the smallest $|M_{\gamma\pi^+\pi^-} - m_{\eta'}|$ is chosen.

For the $J/\psi \to \gamma \eta' (\to \eta \pi^+ \pi^-, \eta \to \gamma \gamma) \pi^+ \pi^-$ channel,



FIG. 1. The $\eta' \pi^+ \pi^-$ invariant mass spectra after the application of all selection criteria. The plot on the left side shows the spectrum for events with the $\eta' \to \gamma \pi^+ \pi^-$ channel; that on the right shows the spectrum for the $\eta' \to \eta (\to \gamma \gamma) \pi^+ \pi^-$ channel. In both plots, the dots with error bars are data, the shaded histograms are the background, the solid histograms are phase space (PHSP) MC events of $J/\psi \to \gamma \eta' \pi^+ \pi^-$ (arbitrary normalization), the dotted vertical line shows the position of $p\bar{p}$ mass threshold.

a 4C kinematic fit to the $\gamma\gamma\gamma\pi^{+}\pi^{-}\pi^{+}\pi^{-}$ hypothesis is performed; events with $\chi^{2}_{4C} < 40$ are accepted. If there are more than three photon candidates, the three that minimize χ^{2}_{4C} are retained. To suppress backgrounds from $\pi^{0} \rightarrow \gamma\gamma$, events in which any one of the three two-photon pairings satisfies $|M_{\gamma\gamma} - m_{\pi^{0}}| <$ $40 \text{ MeV}/c^{2}$ are rejected. The η is reconstructed by the two photons that best satisfy $|M_{\gamma\gamma} - m_{\eta}| < 30 \text{ MeV}/c^{2}$. A five-constraint (5C) kinematic fit, energy-momentum conservation with an additional constraint on the $\eta \rightarrow$ $\gamma\gamma$ invariant mass to be equal to m_{η} , is performed, and $\chi^{2}_{5C} < 40$ is required. Then the η' candidate is formed from the $\eta\pi^{+}\pi^{-}$ combination that best satisfies $|M_{\eta\pi^{+}\pi^{-}} - m_{\eta'}| < 10 \text{ MeV}/c^{2}$.

The $\eta' \pi^+ \pi^-$ invariant mass spectra of the surviving events are shown in Fig. 1, where peaks corresponding to the X(1835), X(2120), X(2370), η_c [2], and a structure near 2.6 GeV/ c^2 that has not been seen before are evident for both η' decays. Thanks to the high statistical precision, an abrupt change in slope of the X(1835) line shape at the $p\bar{p}$ mass threshold is evident in both event samples.

An inclusive sample of $10^9 J/\psi$ decays events that are generated according to the Lund-Charm model [23] and Particle Data Group (PDG) [24] decay tables, is used to study potential background processes. These include events with no real η 's in the final state (non- η ') and those from $J/\psi \rightarrow \pi^0 \eta' \pi^+ \pi^-$. We use η' mass sideband events to estimate the non- η' background contribution to the $\eta' \pi^+ \pi^-$ invariant mass distribution. For the $J/\psi \rightarrow \pi^0 \eta' \pi^+ \pi^-$ background, we use a one-dimensional data-driven method that first selects $J/\psi \rightarrow \pi^0 \eta' \pi^+ \pi^-$ from the data to determine the shape of their contribution to the selected $\eta' \pi^+ \pi^-$ mass spectrum and re-weight this shape by the ratio of MC-determined efficiencies for $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$ and $J/\psi \rightarrow \pi^0 \eta' \pi^+ \pi^-$ events; the total weight after re-weighting is the estimated number of $J/\psi \rightarrow \pi^0 \eta' \pi^+ \pi^-$ background events. Our studies of background processes show that neither the four peaks mentioned above nor the abrupt change in the line shape at $2m_p$ are caused by background processes.

We perform simultaneous fits to the $\eta' \pi^+ \pi^-$ invariant mass distributions between 1.3 GeV/c^2 and 2.25 GeV/c^2 for both selected event samples with the $f_1(1510)$, X(1835) and X(2120) peaks represented by three efficiency-corrected Breit-Wigner functions convolved with a Gaussian function to account for the mass resolution, where the Breit-Wigner masses and widths are free parameters. The non-resonant $\eta' \pi^+ \pi^$ contribution is obtained from Monte-Carlo simulation; the non- η' and $J/\psi \rightarrow \pi^0 \eta' \pi^+ \pi^-$ background contributions are obtained as discussed above. For resonances and the non-resonant $\eta' \pi^+ \pi^-$ contribution, the phase space for $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$ is considered: according to the J^P of $f_1(1510)$ and $X(1835), J/\psi \rightarrow$ $\gamma f_1(1510)$ and $J/\psi \rightarrow \gamma X(1835)$ are S-wave and *P*-wave processes, respectively; all other processes are assumed to be S-wave processes. Without explicit mention, all components are treated as incoherent contributions. In the simultaneous fits, the masses and widths of resonances, as well as the branching fraction for J/ψ radiative decays to $\eta' \pi^+ \pi^-$ final states (including resonances and non-resonant $\eta' \pi^+ \pi^-$) are constrained to be the same for both η' decay channels. The fit results are shown in Fig. 2, where it is evident that using a

5

simple Breit-Wigner function to describe the X(1835)line shape fails near the $p\bar{p}$ mass threshold. The log \mathcal{L} (\mathcal{L} is the combined likelihood of simultaneous fits) of this fit is 630503.3. Typically, there are two circumstances where an abrupt distortion of a resonance's line shape shows up: a threshold effect caused by the opening of an additional decay mode; or interference between two resonances. We tried to fit the data for both of these possibilities.



FIG. 2. Fit results with simple Breit-Wigner formulae. The dashed dotted vertical line shows the position of $p\bar{p}$ mass threshold, the dots with error bars are data, the solid curves are total fit results, the dashed curves are the X(1835), the short-dashed curves the $f_1(1510)$, the dash-dot curves the X(2120), and the long-dashed curves are the non-resonant $\eta'\pi^+\pi^-$ fit results; the shaded histograms are background events. The inset shows the data and the global fit between 1.8 GeV/ c^2 and 1.95 GeV/ c^2 .

In the first model, we assume the state around 1.85 GeV/c^2 couples to $p\bar{p}$. The line shape of $\eta'\pi^+\pi^-$ above the $p\bar{p}$ threshold is therefore affected by the opening of the $X(1835) \rightarrow p\bar{p}$ decay channel, similar to the distortion of the $f_0(980) \rightarrow \pi^+\pi^-$ line shape at the $K\bar{K}$ threshold. To study this, the Flatté formula [25] is used for the X(1835) line shape:

$$T = \frac{\sqrt{\rho_{\text{out}}}}{\mathcal{M}^2 - s - i \sum_k g_k^2 \rho_k}.$$
 (1)

Here T is the decay amplitude, ρ_{out} is the phase space for $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$, \mathcal{M} is a parameter with the dimension of mass, s is the square of the $\eta' \pi^+ \pi^-$ system's mass, ρ_k is the phase space for decay mode k, and g_k^2 is the corresponding coupling strength. The term $\sum_k g_k^2 \rho_k$ describes how the decay width varies with s. Approximately:

$$\sum_{k} g_k^2 \rho_k \approx g_0^2 \left(\rho_0 + \frac{g_{p\bar{p}}^2}{g_0^2} \rho_{p\bar{p}} \right), \qquad (2)$$

where g_0^2 is the sum of g^2 of all decay modes other than $X(1835) \rightarrow p\bar{p}, \rho_0$ is the maximum two-body decay phase space volume [24] and $g_{p\bar{p}}^2/g_0^2$ is the ratio between the coupling strength to the $p\bar{p}$ channel and the sum of all other channels.

The fit results for this model are shown in Fig. 3. The Flattè model fit has a $\log \mathcal{L} = 630549.5$ that is



FIG. 3. Fit results of using Flatté formula. The dashed dotted vertical line shows the position of $p\bar{p}$ mass threshold, the dots with error bars are data, the solid curves are total fit results, the dashed curves are the state around 1.85 GeV/ c^2 , the short-dashed curves are the $f_1(1510)$, the dash-dotted curves are the X(2120), the dash-dot-dot-dotted curves are X(1920), and the long-dashed curves are non-resonant $\eta'\pi^+\pi^-$ fit results; the shaded histograms are background events. The inset shows the data and the global fit between 1.8 GeV/ c^2 and 1.95 GeV/ c^2 .

improved over the simple Breit-Wigner one by 46, so the significance of $g_{p\bar{p}}^2/g_0^2$ being non-zero is 9.6σ . In the fit, an additional Breit-Wigner resonance (denoted as "X(1920)" in Fig. 3) is needed with a mass of 1918.6±3.0 MeV/ c^2 and width of 50.6 ± 20.9 MeV/ c^2 ; the statistical significance of this peak is 5.7σ . In the simple Breit-Wigner fit, the significance of X(1920) is negligible. The fit yields $\mathcal{M} = 1638.0 \pm 121.9$ MeV/ c^2 , $g_0^2 =$ 93.7 ± 35.4 (GeV/ c^2)², $g_{p\bar{p}}^2/g_0^2 = 2.31 \pm 0.37$, a product branching fraction of $\mathcal{B}(J/\psi \to \gamma X) \cdot \mathcal{B}(X \to \eta' \pi^+ \pi^-) =$ $(3.93 \pm 0.38) \times 10^{-4}$. The value of $g_{p\bar{p}}^2/g_0^2$ implies that the couplings between the state around 1.85 GeV/ c^2 and the $p\bar{p}$ final states is very large. Following the definitions given in Ref. [26], the pole position is determined by requiring the denominator in Eq. 1 to be zero. The pole nearest to the $p\bar{p}$ mass threshold is found to be $M_{\rm pole} = 1909.5 \pm 15.9 \text{ MeV}/c^2$ and $\Gamma_{\rm pole} = 273.5 \pm 21.4 \text{ MeV}/c^2$. Taking the systematic uncertainties (see below) into account, the significance of $g_{p\bar{p}}^2/g_0^2$ being non-zero is larger than 7σ .

In the second model, we assume the existence of a narrow resonance near the $p\bar{p}$ threshold and that the interference between this resonance and the X(1835) produces the line shape distortion. Here we denote this narrow resonance as "X(1870)." For this case we represent the line shape in the vicinity on 1835 MeV by the square of T, where

$$T = \left(\frac{\sqrt{\rho_{\text{out}}}}{M_1^2 - s - iM_1\Gamma_1} + \frac{\beta e^{i\theta}\sqrt{\rho_{\text{out}}}}{M_2^2 - s - iM_2\Gamma_2}\right).$$
 (3)

Here, ρ_{out} and s have the same meaning as they had in Eq. 1; M_1 , Γ_1 , M_2 and Γ_2 represent the masses and widths of the X(1835) and X(1870) resonances respectively; and β and θ are the relative $\eta' \pi^+ \pi^$ coupling strengths and the phase between the two resonances.

The fit results for the second model are shown in Fig. 4. The log \mathcal{L} of this fit is 630540.3, which is improved by 37 with 4 additional parameters over that for the fit using one simple Breit-Wigner. The X(1835) mass is $1825.3 \pm$ 2.4 MeV/ c^2 and width is 245.2 \pm 13.1 MeV/ c^2 ; The X(1870) mass is 1870.2 ± 2.2 MeV/ c^2 and width is $13.0 \pm$ 6.1 MeV/ c^2 , with a statistical significance that is 7.9 σ . It is known that there are two non-trivial solutions in a fit using a coherent sum of two Breit-Wigner functions [27]. In the parameterization of Eq. 3, the two solutions share the same M_1 , Γ_1 , M_2 and Γ_2 , but have different values of β and θ , which means that the only observable difference between the solutions are branching fractions of the two Breit-Wigner functions. The product branching fractions with constructive interference are $\mathcal{B}(J/\psi \rightarrow$ $\gamma X(1835)) \cdot \mathcal{B}(X(1835) \to \eta' \pi^+ \pi^-) = (3.01 \pm 0.17) \times 10^{-4}$ and $\mathcal{B}(J/\psi \rightarrow \gamma X(1870)) \cdot \mathcal{B}(X(1870) \rightarrow \eta' \pi^+ \pi^-) =$ $(2.03 \pm 0.12) \times 10^{-7}$, while the solution with destructive interference gives $\mathcal{B}(J/\psi \rightarrow \gamma X(1835)) \cdot \mathcal{B}(X(1835) \rightarrow$ $\eta'\pi^+\pi^-) = (3.72 \pm 0.21) \times 10^{-4}$, and $\mathcal{B}(J/\psi \rightarrow 0.21) \times 10^{-4}$ $\gamma X(1870)) \cdot \mathcal{B}(X(1870) \rightarrow \eta' \pi^+ \pi^-) = (1.57 \pm 0.09) \times$ 10^{-5} . In this model, the X(1920) is not included in the fit because its significance is just 3.9σ . Considering systematic uncertainties (see below), the significance of X(1870) is larger than 7σ .

The systematic uncertainties come from data-MC differences in the tracking, photon detection and particle identification efficiencies, the kinematic fit, requirements on the invariant mass distribution of $\gamma\gamma$, signal selection of ρ^0 , η and η' , total number of J/ψ events, branching fractions for intermediate states decays, fit ranges, background descriptions, mass resolutions, and



FIG. 4. Fit results of using a coherent sum of two Breit-Wigner amplitudes. The dashed dotted vertical line shows the position of $p\bar{p}$ mass threshold, the dots with error bars are data, the solid curves are total fit results, the dashed curves are the sum of X(1835) and X(1870), the short-dashed curves are the $f_1(1510)$, the dash-dotted curves are the X(2120), the long-dashed curves are non-resonant $\eta' \pi^+ \pi^-$ fit results, the shaded histograms are background events. The inset shows the data and the global fit between 1.8 GeV/ c^2 and 1.95 GeV/ c^2 .

TABLE I. Fit results of using Flatté formula. The first errors are statistical errors, the second errors are systematic errors; the branching ratio is the product of $\mathcal{B}(J/\psi \to \gamma X)$ and $\mathcal{B}(X \to \eta' \pi^+ \pi^-)$.

| The state around 1.85 GeV/c^2 | |
|--|--|
| $\mathcal{M} \; ({ m MeV}/c^2)$ | $1638.0 \pm 121.9^{+127.8}_{-254.3}$ |
| $g_0^2 \; (({ m GeV}/c^2)^2)$ | $93.7 \pm 35.4^{+47.6}_{-43.9}$ |
| $g_{par p}^2/g_0^2$ | $2.31 \pm 0.37^{+0.83}_{-0.60}$ |
| $M_{\rm pole}~({\rm MeV}/c^2)$ | $1909.5 \pm 15.9^{+9.4}_{-27.5}$ |
| $\Gamma_{\rm pole} \ ({\rm MeV}/c^2)$ | $273.5 \pm 21.4^{+6.1}_{-64.0}$ |
| Branching Ratio | $(3.93 \pm 0.38^{+0.31}_{-0.84}) \times 10^{-4}$ |

intermediate structure of $\pi^+\pi^-$. In the first model, the dominant terms are the fit range, the background description and the intermediate structure of $\pi^+\pi^-$. Considering all systematic uncertainties, the final result is shown in Table I. For the second model, the dominant two systematic sources are the background description and the intermediate structure of $\pi^+\pi^-$. Considering all systematic uncertainties, the final result is shown in Table II.

In summary, the $J/\psi \to \gamma \eta' \pi^+ \pi^-$ process is studied

TABLE II. Fit results using a coherent sum of two Breit-Wigner amplitudes. The first errors are statistical errors, the second errors are systematic errors; the branching ratio is the product of $\mathcal{B}(J/\psi \to \gamma X)$ and $\mathcal{B}(X \to \eta' \pi^+ \pi^-)$.

| X(1835) | |
|----------------------------------|--|
| Mass (MeV/c^2) | $1825.3 \pm 2.4^{+17.3}_{-2.4}$ |
| Width (MeV/c^2) | $245.2 \pm 13.1^{+4.6}_{-9.6}$ |
| B.R. (constructive interference) | $(3.01\pm0.17^{+0.26}_{-0.28})\times10^{-4}$ |
| B.R. (destructive interference) | $(3.72\pm0.21^{+0.18}_{-0.35})\times10^{-4}$ |
| X(1870) | |
| Mass (MeV/c^2) | $1870.2 \pm 2.2^{+2.3}_{-0.7}$ |
| Width (MeV/c^2) | $13.0\pm6.1^{+2.1}_{-3.8}$ |
| B.R. (constructive interference) | $(2.03\pm0.12^{+0.43}_{-0.70})\times10^{-7}$ |
| B.R. (destructive interference) | $(1.57 \pm 0.09^{+0.49}_{-0.86}) \times 10^{-5}$ |

with $1.09 \times 10^9 J/\psi$ events collected at the BESIII experiment in 2012. We observed a significant distortion of the $\eta' \pi^+ \pi^-$ line shape near the $p\bar{p}$ mass threshold that cannot be accommodated by an ordinary Breit-Wigner resonance function. Two typical models for such a line shape are used to fit the data. The first model assumes the state around 1.85 GeV/ c^2 couples with $p\bar{p}$ and the distortion reflects the opening of the $p\bar{p}$ decay channel. The fit result for this model yields a strong coupling between the broad structure and the $p\bar{p}$ of $g_{p\bar{p}}^2/g_0^2 = 2.31 \pm 0.37^{+0.83}_{-0.60}$, with a statistical significance larger than 7σ for being non-zero. The pole nearest to the $p\bar{p}$ mass threshold of this state is located at $M_{\rm pole}$ = $M_{\rm pole} = 1909.5 \pm 15.9(\text{stat.})^{+9.4}_{-27.5}(\text{syst.}) \text{ MeV}/c^2 \text{ and } \Gamma_{\rm pole} = 273.5 \pm 21.4(\text{stat.})^{+6.1}_{-64.0}(\text{syst.}) \text{ MeV}/c^2.$ The second model assumes the distortion reflects interference between the X(1835) and another resonance with mass close to the $p\bar{p}$ mass threshold. A fit with this model uses a coherent sum of two interfering Breit-Wigner amplitudes to describe the $\eta' \pi^+ \pi^-$ mass spectrum around 1.85 GeV/ c^2 . This fit yields a narrow resonance below the $p\bar{p}$ mass threshold with $M = 1870.2 \pm 2.2 (\text{stat.})^{+2.3}_{-0.7} (\text{syst.}) \text{ MeV}/c^2$ and $\Gamma = 13.0 \pm 6.1 (\text{stat.})^{+2.1}_{-3.8} (\text{syst.}) \text{ MeV}/c^2$, with a statistical significance larger than 7σ . With current data, both models fit the data well with fit qualities, and both suggest the existence of a state, either a broad state with strong couplings to $p\bar{p}$, or a narrow state just below the $p\bar{p}$ mass threshold. For the broad state above the $p\bar{p}$ mass threshold, its strong couplings to $p\bar{p}$ suggests the existence of a $p\bar{p}$ molecule-like state. For the narrow state just below $p\bar{p}$ mass threshold, its very narrow width suggests that it be an unconventional meson, most likely a $p\bar{p}$ bound state. So both fits support the existence of a $p\bar{p}$ molecule-like or bound state. With current statistics, more sophisticated models such as a mixture of above two models cannot be ruled out. In order to elucidate further

the nature of the states around 1.85 GeV/ c^2 , more data are needed to further study $J/\psi \rightarrow \gamma \eta' \pi^+ \pi^-$ process. Also, line shapes for other decay modes should be studied near the $p\bar{p}$ mass threshold, including further studies of $J/\psi \rightarrow \gamma p\bar{p}$ and $J/\psi \rightarrow \gamma \eta K_S^0 K_S^0$.

The BESIII collaboration thanks the staff of BEPCII and the IHEP computing center for their strong support. This work is supported in part by National Key Basic Research Program of China under Contract No. 2015CB856700; National Natural Science Foundation of China (NSFC) under Contracts Nos. 11235011. 11322544, 11335008, 11425524; the Chinese Academy of Sciences (CAS) Large-Scale Scientific Facility Program; the CAS Center for Excellence in Particle Physics (CCEPP); the Collaborative Innovation Center for Particles and Interactions (CICPI); Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contracts Nos. U1232201, U1332201; CAS under Contracts Nos. KJCX2-YW-N29, KJCX2-YW-N45; 100 Talents Program of CAS; National 1000 Talents Program of China; INPAC and Shanghai Key Laboratory for Particle Physics and Cosmology; Istituto Nazionale di Fisica Nucleare, Italy; Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contract U1532257; Joint Large-Scale Scientific Facility No. Funds of the NSFC and CAS under Contract No. U1532258; Koninklijke Nederlandse Akademie van Wetenschappen (KNAW) under Contract No. 530-4CDP03; Ministry of Development of Turkey under Contract No. DPT2006K-120470; The Swedish Resarch Council; U. S. Department of Energy under Contracts Nos. DE-FG02-05ER41374, DE-SC-0010504, DE-SC0012069, DESC0010118; U.S. National Science University of Groningen (RuG) and Foundation; Helmholtzzentrum fuer Schwerionenforschung the GmbH (GSI), Darmstadt; WCU Program of National Research Foundation of Korea under Contract No. R32-2008-000-10155-0.

- M. Ablikim *et al.* (BES Collaboration), Phys. Rev. Lett. 95, 262001 (2005).
- [2] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. **106**, 072002 (2011).
- [3] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. **115**, 091803 (2015).
- [4] J. Z. Bai *et al.* (BES Collaboration), Phys. Rev. Lett. **91**, 022001 (2003).
- [5] M. Ablikim *et al.* (BESIII Collaboration), Chin. Phys. C 34, 421 (2010).
- [6] J. P. Alexander *et al.* (CLEO Collaboration), Phys. Rev. D 82, 092002 (2010).
- [7] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. **108**, 112003 (2012).

- [8] T. Huang and S. L. Zhu, Phys. Rev. D 73, 014023 (2006).
- [9] N. Kochelev and D. P. Min, Phys. Lett. B 633, 283 (2006).
- [10] G. Hao, C. F. Qiao, and A. Zhang, Phys. Lett. B 642, 53 (2006).
- [11] B. A. Li, Phys. Rev. D 74, 034019 (2006).
- [12] X. H. Liu et al., Phys. Rev. D 80, 034032 (2009).
- [13] S. L. Zhu and C. S. Gao, Commun. Theor. Phys. 46, 291 (2006).
- [14] J. P. Dedonder, B. Loiseau, B. El-Bennich, and S. Wycech, Phys. Rev. C 80, 045207 (2009).
- [15] G. J. Ding, R. G. Ping, and M. L. Yan, Eur. Phys. J. A 28, 351 (2006).
- [16] C. Liu, Eur. Phys. J. C 53, 413 (2008).
- [17] Z. G. Wang and S. L. Wan, J. Phys. G 34, 505 (2007).
- [18] M. Ablikim *et al.* (BESIII Collaboration), Chin. Phys. C 36, 915 (2012).

- [19] M. Ablikim *et al.* (BESIII Collaboration), Nucl. Instrum. Meth. A **614**, 345 (2010).
- [20] J. Z. Bai *et al.* (BES Collaboration), Nucl. Instrum. Meth. A **344**, 319 (1994); Nucl. Instrum. Meth. A **458**, 627 (2001).
- [21] S. Agostinelli *et al.* (GEANT4 Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
- [22] S. Jadach, B. F. L. Ward, and Z. Was, Comput. Phys. Commun. 130, 260 (2000); Phys. Rev. D 63, 113009 (2001).
- [23] J. C. Chen et al., Phys. Rev. D 62, 034003 (2000).
- [24] K. A. Olive *et al.* (Particle Data Group), Chin. Phys. C 38, 090001 (2014).
- [25] S. M. Flatté, Phys. Lett. B 63, 224 (1976).
- [26] B. S. Zou and D. V. Bugg, Phys. Rev. D 48, R3948 (1993).
- [27] K. Zhu, X. H. Mo, C. Z. Yuan, and P. Wang, Int. J. Mod. Phys. A 26, 4511 (2011).