# SINGLE PEAK DIFFERENTIAL THERMOLUMINESCENCE METHOD FOR CALCULATION OF THE TRAP ENERGIES 

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#### Abstract

The energy level of the traps of natural calcium fluorite sample is calculated using a single thermoluminescence glow curve peak by new non-isothermal kinetic method. The plot of $\operatorname{Ln}\left(\frac{d a}{d T} \frac{1}{1-a}\right)$ versus $\frac{1}{T}$ yields a straight line with a alope of $-\frac{E}{k}$, where $E$ is the trap energy $k$, is the Boltzman constant, " $a$ " is the fraction of the total occupied trap number. The frequency factor $S$ can be calculated from $y$ intercept which is equal to $L n(S x b)$ where $b$ is the constant heating rate.

The trap energy value of the main glow curve peak of the natural calcium fluorite is calculated as 0.64 eV by using single peak differential thermoluminescence method.


## ÖZET

Tabii kalsiyum florïrün tuzak enerjilerini tayin için yeni bir değişen sıcaklık metodu uygulanmıştır. Bu metoda göre $\operatorname{Ln}\left(\frac{d a}{d T} \frac{1}{1-a}\right)$ bağıntısını $1 / T$ nin fonksiyonu olarak gösteren grafik bir doğru denklemi vermekte ve bu doğrunun eğiminin $\left(-\frac{E}{k}\right)$ değerine eşit olması özelliğinden $E$ tuzak enerjisi tayin edilebilmektedir. Kalsiyum florüriün ana piki için $E=0.64 \mathrm{eV}$ değeri bulunmuştur.

## DEFINATION OF THE METHOD

Since the method applied should be used for a single peak of the thermoluminescence glow curve (monoenergetic traps) is named as "Single Peak Differential Method ${ }^{11}$.

As known from Randall-Wilkins ${ }^{2}$ thermoluminescence model light intencity was given for isothermal experiments as

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$$
\begin{equation*}
\mathrm{I}=-\mathrm{C} \frac{\mathrm{dn}}{\mathrm{dt}} \tag{1}
\end{equation*}
$$

\]

where n is the number of the occupied traps at time t and C is the proportionality constant. Integration of this equation, if $n_{0}$ is the initial number of occupied traps at time zero

$$
\begin{equation*}
\int_{0}^{t} I d t=-\int_{n_{0}}^{n} C d n \tag{2}
\end{equation*}
$$

The left side of the equation 2 is the area under the glow curve in the time interval of $(o-t)$. So

$$
\begin{equation*}
A_{1}=C\left(n_{0}-n\right)=C n_{0}-C n=A-A_{2} \tag{3}
\end{equation*}
$$

is obtained by abbriviating A as the whole area under the glow curve peak and $\mathrm{A}_{2}$ as the area completing the $A_{1}$ to the $A$ value as shown in Figure-1. As a result the area under the glow curve peak is proportional to the occupied trap number at that moment. From the equation 3
$\mathrm{A}_{2}=\mathrm{Cn} \quad$ can be drived. Differentiating the equation

$$
\begin{gather*}
\frac{\mathrm{dA}_{2}}{\mathrm{dt}}=\mathrm{C} \frac{\mathrm{dn}}{\mathrm{dt}} \quad \text { is obtained }  \tag{4}\\
\text { Since }-\frac{\mathrm{dn}}{\mathrm{dt}}=\mathrm{pn} \tag{5}
\end{gather*}
$$

was given by Randall-Wilkins model if $n$ was the occupied trap number, $p$ was the probability. Combination of the equation 3,4 and 5 yields

$$
\begin{equation*}
-\frac{\mathrm{dA}_{2}}{\mathrm{dt}}=\mathrm{A}_{2} \mathrm{p} \tag{6}
\end{equation*}
$$

As seen from Figure-1

$A=A_{1}+A_{2}$ is given. $A_{1}$ and $A_{2}$ variables and $A$ is constant so differentiation of this equation yields

$$
\begin{equation*}
-\frac{\mathrm{dA}_{2}}{\mathrm{dt}}=\frac{\mathrm{dA}_{1}}{\mathrm{dt}} \tag{7}
\end{equation*}
$$

For the lineer heating rates this equation can be modified (by using $\frac{d T}{d t}=b$ equation) as

$$
\begin{equation*}
b \frac{\mathrm{dA}_{1}}{\mathrm{dT}}=\left(\mathrm{A}-\mathrm{A}_{1}\right) \mathrm{p} \tag{8}
\end{equation*}
$$

dividing by A and defining $\frac{\mathrm{A}_{1}}{\mathrm{~A}}=\mathrm{a}$

$$
\begin{equation*}
\frac{b}{A} \frac{d A_{1}}{d T}=(1-a) p \quad \text { is obtained } \tag{9}
\end{equation*}
$$

Since " a " was defined as $\mathrm{a}=\frac{\mathrm{A}_{1}}{\mathrm{~A}}$ differential of the equation can be obtained as

$$
\frac{\mathrm{da}}{\mathrm{dT}}=\frac{1}{\mathrm{~A}} \frac{\mathrm{dA}_{1}}{\mathrm{dT}}
$$

The value of $\frac{\mathrm{dA}_{1}}{\mathrm{dT}}$ can be derived and place into equation 8

$$
\begin{equation*}
\frac{d a}{d T} \frac{1}{(1-a)}=\frac{p}{b} \quad \text { can be obtained } \tag{10}
\end{equation*}
$$

Probability p was given by Randall-Wilkins as

$$
p=S \exp \left(-\frac{E}{k T}\right)
$$

where $k$ is the Blotzman constant, $S$ is the Frequency factor $E$ is the trap energy, T is the absolute temperature of the sample. Having natural logarithm of the equation 10

$$
\begin{equation*}
\operatorname{Ln}\left(\frac{\mathrm{da}}{\mathrm{dT}} \frac{1}{(1-\mathrm{a})}\right)=-\frac{\mathrm{E}}{\mathrm{kT}}+\operatorname{Ln} \mathrm{S}-\operatorname{Ln} \mathrm{b} \quad \text { is obtained } \tag{11}
\end{equation*}
$$

The plot of $\operatorname{Ln}\left(\frac{d a}{d T} \frac{1}{(1-a)}\right)$ versus $\frac{1}{T}$ yields a straight line having a slope of $(E / k)$ and $y$ intercept which is equal to $(\operatorname{Ln} S-\operatorname{Ln} b)$.

## APPLICATION OF THE METHOD

The data obtained from the main peak of the glow curve of the natural calcium fluorite phosphore (numbered 18 blue) which is shown in Figure-2 is tabulated in Table-1 which contains the heights measured from the curve and the areas ( $\mathrm{A}_{1}$ ) calculated by Library program 10 of TI- 58 or 59 calculator. ' a ' values can be calculated dividing partial areas $A_{1}$ by the whole area under the glow curve peak.


Figure - 2

Table: 1
( $\mathrm{a}-\mathrm{T}$ ) Data Obtained From The Main Peak of The Glow Curve Of The Natural CALCIUM FLUORITE (No: 18, Blue)

| $\begin{aligned} & \mathrm{b}=2.36 \mathrm{C}^{\circ} / \mathrm{sec} \\ & \mathrm{~T}_{0}=459.95 \mathrm{~K}^{\circ} \\ & \mathrm{T}_{\mathrm{m}}=546.91 \mathrm{~K}^{\circ} \end{aligned}$ |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| T K ${ }^{\circ}$ | a | $(1 / \mathrm{T}) 10^{5}$ | Area | I (mm) | $\operatorname{Ln}\left(\frac{d a}{d T} \times \frac{1}{(1-a)}\right)$ |
| 459.95 | 0.00000 | 217.41 | 00000.00 | 000.- |  |
| 474.45 | 0.02247 | 210.77 | 243.96 | 23 |  |
| 488.94 | 0.06341 | 204.52 | 688.4 | 41 |  |
| 496.19 | 0.09513 | 201.54 | 1032.8 | 54 |  |
| 503.43 | 0.13528 | 198.64 | 1468.6 | 66 | -4.984 |
| 517.93 | 0.24207 | 193.08 | 2628 | 94 | -4.466 |
| 525.17 | 0.30952 | 190.41 | 3360.25 | 108 | - 4.245 |
| 533.42 | 0.38514 | 187.82 | 4181.2 | 117 | -4.029 |
| 539.67 | 0.46495 | 185.29 | 5047.58 | 122 | - 3.859 |
| 546.91 | 0.54734 | 182.85 | 5942 | 124 | -- 3.681 |
| 554.16 | 0.62914 | 180.45 | 6830.1 | 121 | - 3.510 |
| 561.41 | 0.70709 | 178.12 | 7676.3 | 110 | -3.344 |
| 568.65 | 0.77654 | 175.85 | 8430.3 | 98 |  |
| 575.9 | 0.83725 | 173.64 | 9089.4 | 83 |  |
| 583.14 | 0.88733 | 171.48 | 9632.2 | 67 |  |
| 590.39 | 0.92674 | 169.38 | 10060.95 | 51 |  |
| 619.38 | 1.00000 | 161.45 | 10856.28 | 10.5 |  |



Figure - 3
The plot of " $a$ " versus $T$ is shown in Figure-3. $a=F(T)$ function should be defined to calculate the da/dT values for the different temperature values. In this work it is thought to fit this curve to a polinominal in the third order in the interval of ' a " value as shown below.

$$
\begin{equation*}
\mathrm{a}=\mathrm{A}+\mathrm{BT}+\mathrm{CT}^{2}+\mathrm{DT}^{3} \tag{12}
\end{equation*}
$$

Substituting the values of $T_{1}, T_{2}, T_{3}, T_{4}$ and corresponding values of $a_{1}, a_{2}$, $\mathrm{a}_{3}, \mathrm{a}_{4}$ into this function, the lineer equation of

$$
\begin{align*}
& \mathrm{a}_{1}=\mathrm{A}+\mathrm{BT}_{1}+\mathrm{CT}_{1}^{2}+\mathrm{DT}_{1}^{3} \\
& \mathrm{a}_{2}=\mathrm{A}+\mathrm{BT}_{2}+\mathrm{CT}_{2}^{2}+\mathrm{DT}_{2}^{3}  \tag{13}\\
& \mathrm{a}_{3}=\mathrm{A}+\mathrm{BT}_{3}+\mathrm{CT}_{3}^{2}+\mathrm{DT}_{3}^{3} \\
& \mathrm{a}_{4}=\mathrm{A}+\mathrm{BT}_{4}+\mathrm{CT}_{4}^{2}+\mathrm{DT}_{4}^{3}
\end{align*}
$$

is obtained.
From this equation the coefficients of A, B, C, D, can be defined in an interval of $\left(a_{1}-a_{4}\right)$. So the function of a $F(T)$ and so the derivative function da/dT can be obtained.

## RESULTS

In the interval of $0.13528 \leqslant a \leqslant 0.38514$ the a $F(T)$ function is

$$
\mathrm{a}=80.67-438.48 \times 10^{-3} \mathrm{~T}+776.89 \times 10^{-6} \mathrm{~T}^{2}-444.30 \times 10^{-9} \mathrm{~T}^{3}
$$

and derivative function is

$$
\frac{\mathrm{da}}{\mathrm{dT}}=438.48 \times 10^{-3}+1552.78 \times 10^{-6} \mathrm{~T}-1332.90 \times 10^{-9} \mathrm{~T}^{2}
$$

In the interval of $0.38514 \leqslant \mathrm{a} \leqslant 0.70709$ the function a $\mathrm{F}(\mathrm{T})$ is

$$
\mathrm{a}=217.47-1216.40 \times 10^{-3} \mathrm{~T}-2251.66 \times 10^{-6} \mathrm{~T}^{2}-1376.40 \times 10^{-9} \mathrm{~T}^{3}
$$

and derivative function is

$$
\frac{\mathrm{da}}{\mathrm{dT}}=1216.40 \times 10^{-3}+4503.32 \times 10^{-6} \mathrm{~T}+4129.20 \times 10^{-9} \mathrm{~T}^{2}
$$

The values of $\operatorname{Ln}\left(\frac{d a}{d T} \times \frac{1}{1-a}\right)$ versus $\frac{1}{T}$ yields a straight line as seen in Figure-4. The slope of this line is calculated as $\mathbf{- 7 4 3 6 . 6 8}$ and then, since this value is equal to $-\frac{\mathrm{E}}{\mathrm{k}}\left(\mathrm{k} 8.61 \times 10^{-5} \mathrm{eV} / \mathrm{K}^{\circ} \mathrm{mol}\right.$. $)$
$\mathrm{E}=0.64 \mathrm{eV}$ is found in the interval of $0.24 \leqslant \mathrm{a} \leqslant 0.71$.


Figure - 4

## DISCUSSION

This method is applied to natural calcium fluorite phosphore together with other two method. One of them is Garlick-Gibson ${ }^{3}$ method which yields 0.64 eV trap energy value. This value fits the result obtained by that method. The second method is "Single Peak Integration Method" ${ }^{4}$ which is also introduced together with the method used in that work. 0.54 eV trap energy value is obtained by that second method.

Although the application of that method takes a long time but it is most belivable since substantial part of the peak is used.

## REFERENCES

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